

HEYTING-OCKHAM LOGIC AND HYPERINTENTIONALITY

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The logic HYPE was recently [3] suggested by H. Leitgeb with the aim to give a basic propositional logic allowing to deal with hyperintensional contexts. The approach to negation in HYPE is a combination of ‘Star’ and ‘Perp’ from [2], where J.M. Dunn denoted in this way two basic approaches for treatment of the negation operation, via *-star operator and via the incompatibility relation:

$$\begin{aligned}(\neg^*) \quad w \models \neg\varphi & \text{ iff } w^* \not\models \varphi \\(\neg^\perp) \quad w \models \neg\varphi & \text{ iff } \forall u(u \models \varphi \text{ implies } u \perp w)\end{aligned}$$

Moreover, the negation of HYPE has also features of strong negation [4]. A complex combination of conditions involved in the definition of HYPE semantics implies however that the resulting negation operator loses the features of strong negation, moreover, ‘Perp’ turns to ‘Star’.

It turns out that logic HYPE is closely related to Heyting-Ockham logic N^* introduced in [1] as a framework for studying logical foundations of WFS [6] (well founded semantics of logic programs with negation). Algebraic semantics for N^* and the term ‘Heyting-Ockham logic’ were suggested in [5].

In this talk we track the history of ‘Star’ approach to negation, demonstrate that in Vakarelov’s theory [7] of negation N^* can be characterized as the least normal and co-normal logic with intuitionistic impication, and show that proof theoretically hyperintensional HYPE turns out to be equivalent to intensional $N^* + \{\varphi \leftrightarrow \neg\neg\varphi\}$.

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